

Stack client example: Postfix expression evaluation

Infix. Standard way of writing arithmetic expressions, using parentheses for precedence.

Example. $(1+((2+3)*(4*5))) = (1+(5*20)) = 101$

Postfix. Write operator *after* operands (instead of in between them).

Example. $1\ 2\ 3\ +\ 4\ 5\ *\ * +$ **Remarkable fact.** No parentheses are needed!

Jan Łukasiewicz 1878–1956

HP-35 (1972)

First handheld calculator. "Enter" means "push". No parentheses.

Made slide rules obsolete (!)

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also called "reverse Polish" notation (RPN)



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	$1\ 2\ 3\ +\ 4\ 5\ *\ * +$	
	$1\ (2 + 3)\ 4\ 5\ *\ * +$	← find first operator, convert to infix, enclose in ()
	$1\ ((2 + 3) * (4 * 5)) +$	↙ iterate, treating subexpressions in parentheses as atomic
	$(1 + ((2 + 3) * (4 * 5)))$	



makes slide rule obsolete!... but that was a long long time ago!!!

Next. With a stack, postfix expressions are easy to evaluate.

```
public class Postfix
{
    public static void main(String[] args)
    {
        Stack<Double> stack = new Stack<Double>();
        while (!StdIn.isEmpty())
        {

            String token = StdIn.readString();
            if (token.equals("*"))
                stack.push(stack.pop() * stack.pop());
            else if (token.equals("+"))
                stack.push(stack.pop() + stack.pop());
            else if (token.equals("-"))
                stack.push(- stack.pop() + stack.pop());
            else if (token.equals("/"))
                stack.push((1.0/stack.pop()) * stack.pop());
            else if (token.equals("sqrt"))
                stack.push(Math.sqrt(stack.pop()));
            else
                stack.push(Double.parseDouble(token));
        }
        StdOut.println(stack.pop());
    }
}
```